

Notes - Dr. D.K. Jain 24.3.2020 Teaching/Learning from Home

Example 1. Design a short column, square in section, to carry an axial load of 2000 kN using M20 grade concrete and (i) mild steel (ii) Fe 415 grade steel

Solution:-

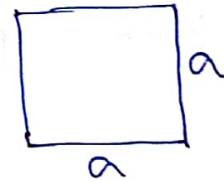
Factored load  $P_u = 2000 \times 1.5 = 3000 \text{ kN}$

Since length is not given, no need to calculate  $e_{min}$ . & since it is a short axial column, so

~~St~~  $P_u = 0.4 f_{ck} \cdot A_c + 0.67 f_y \cdot A_{sc}$  ——— (1)

(i) Mild steel :-  $f_y = 250 \text{ N/mm}^2$

Let us provide a square column with sides = a



For economy, provide min. steel

min. steel = 0.8%

$\therefore A_{sc} = \frac{0.8}{100} \times a \times a = 0.008 a^2$

filling values in formula eq<sup>n</sup> (1), we get

$$\left( \frac{3000}{1000} \right) = 0.4 \times 20 \times a \times a (1 - 0.008) + 0.67 \times 250 \times 0.008 a^2$$

$\left. \begin{aligned} &= (A_g - A_{sc}) \\ &= (A_g - 0.008 A_g) \\ &= A_g (1 - 0.008) \\ &= a \times a (1 - 0.008) \end{aligned} \right\}$

$\therefore a = 568.7 \text{ mm.}$

Provide column of size  $600 \times 600 \text{ mm}$

Gross area provided =  $600 \times 600 = 360000 \text{ mm}^2$  (8)

Gross area required =  $568.7 \times 568.7 = 323419.7 \text{ mm}^2$

Area of longitudinal steel =  $0.008 \times 323419.7$   
 $= 2587 \text{ mm}^2$

provide reinf. bars  $4-20 \phi = 1256 \text{ mm}^2$   
 $+ 8-16 \phi = 1600 \text{ mm}^2$   


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 $2856 \text{ mm}^2 > 2587 \text{ mm}^2$   
 so, OK.

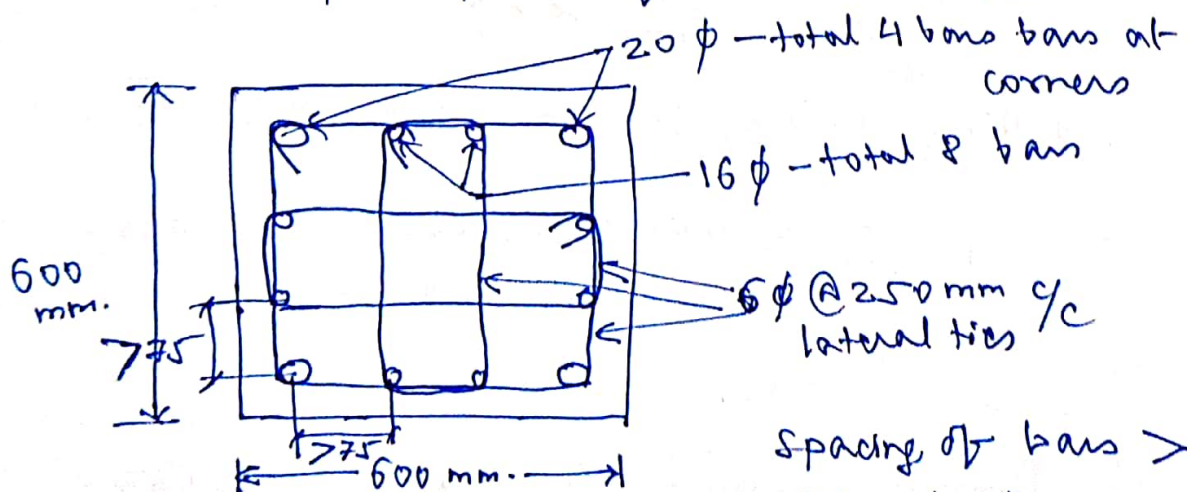
Dia & Pitch of Lateral Ties:-

Dia  $\phi_T \leq \frac{(\phi_L)_{\max}}{4} = \frac{20}{4} = 5 \text{ mm.}$   
 $\leq 6 \text{ mm.}$

so, provide ~~8 mm~~ 6 mm.  $\phi$  bars (in mild steel, min dia = 6 mm)

Pitch  $p \leq$  least lateral dimension = 600 mm.  
 $\leq 16 (\phi_L)_{\min.} = 16 \times 16 = 256 \text{ mm.}$   
 $\leq 300 \text{ mm.}$

so, adopt a pitch of 250 mm. c/c



Spacing of bars  $> 75 \text{ mm}$   
 so extra ties provided

⑧ Fe 415 grade steel  $f_y = 415 \text{ N/mm}^2$  ⑨

Putting values in eq<sup>n</sup> ①, we get

$$3000 \times 1000 = 0.4 \times 20 \times a^2 (1 - 0.008) + 0.67 \times 415 \times 0.008 a^2$$

$$\therefore a = 543.4 \text{ mm.}$$

Adopt column size = 550 mm. x 550 mm.

Gross area of concrete provided = 550 x 550

$$\begin{aligned} \text{Gross area of concrete required} &= 543.4 \times 543.4 \\ &= 2953 \text{ mm}^2 \\ &= 295284 \text{ mm}^2 \end{aligned}$$

$$\begin{aligned} \therefore \text{Area of longitudinal steel} &= 0.008 \times 295284 \\ &= 2362 \text{ mm}^2 \end{aligned}$$

$$\begin{aligned} \text{provide reinf. bars } 8 - 20 \phi &= 8 \times 314 = 2512 \text{ mm}^2 \\ &> 2362 \text{ mm}^2 \\ \text{So, OK} \end{aligned}$$

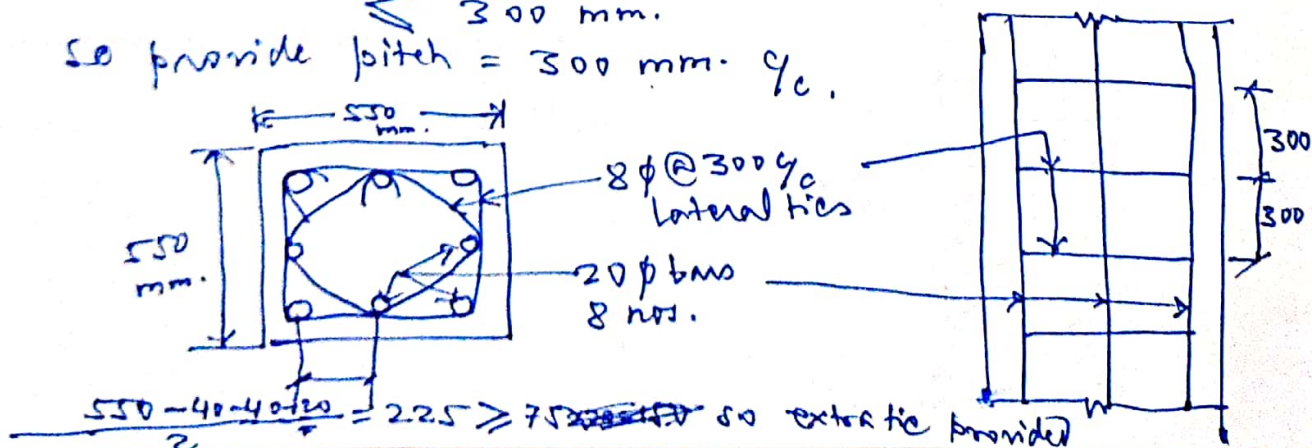
Lateral ties:-

$$\begin{aligned} \text{① Dia } \phi_T &\leq \frac{(\phi_L)_{\max}}{4} = \frac{20}{4} = 5 \text{ mm.} \\ &\leq 6 \text{ mm} \end{aligned}$$

provide 8 mm. dia ties (for Fe415 steel min. dia = 8mm)

$$\begin{aligned} \text{② Pitch } p &\leq \text{least lateral dimension} = 550 \text{ mm.} \\ &\leq 16 (\phi_L)_{\min} = 16 \times 20 = 320 \text{ mm.} \\ &\leq 300 \text{ mm.} \end{aligned}$$

So provide pitch = 300 mm. %c.





Example 2:- Design a short circular column to carry same load i.e. 2000 kN with M20 grade concrete & Fe 415 grade steel.

here  $A_g = \frac{\pi}{4} D^2$

filling values in formula (equation 1), we get,

$$3000 \times 1000 = 0.4 \times 20 \times \left(\frac{\pi}{4} \times D^2\right) (1 - 0.008) + 0.67 \times 415 \times 0.008 \times \frac{\pi}{4} \times D^2$$

$\therefore D = 613 \text{ mm.}$

provide  $D = 625 \text{ mm.}$

Area of steel =  $0.008 \times \frac{\pi}{4} \times 613^2 = 2361 \text{ mm}^2$

Provide 8-20  $\phi$  bars, area =  $8 \times 314 = 2512 > 2361$   
so, ok.

Lateral ties:-

① Dia  $\nless \frac{(\phi_L)_{max}}{4} = \frac{20}{4} = 5 \text{ mm.}$   
 $\nless 6 \text{ mm.}$

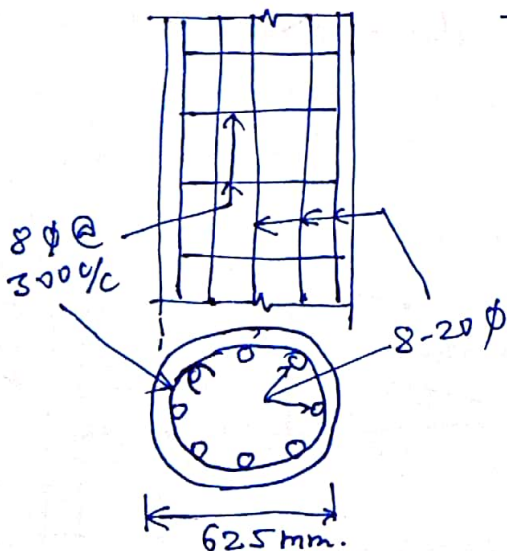
provide 8 mm. dia ties (for Fe 415 steel, min dia = 8 mm)

② Pitch  $\nless$  least lateral dimension =  $D = 625 \text{ mm.}$   
 $\nless 16 (\phi_L)_{min} = 16 \times 20 = 320 \text{ mm.}$   
 $\nless 300 \text{ mm.}$

So, provide pitch = 300 mm.

These are normal ties not spiral ties

Circular Columns with spiral ties has different design procedure which shall be taken up separately.



Example 3:- Design the reinforcement in a column of size 400 mm. x 600 mm subjected to an axial working load of 1800 kN. The column has an unsupported length of 2m. and it is braced against side sway in both the directions & restrained against rotation also. Adopt M20 grade concrete and Fe 415 grade steel.

Solution:-

Column end condition is given as braced against side sway & restrained against rotation at both ends which means both ends are fixed

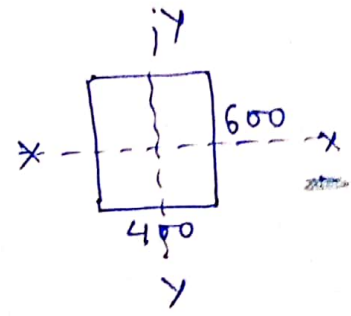
∴ Eff. length  $l_{ex} = l_{ey} = 0.65 l$   
 $= 0.65 \times 2$   
 $= 1.3 \text{ m.}$

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Slenderness ratios:-

$\frac{l_{ex}}{D} = \frac{1.3 \times 1000}{600} = 2.17 < 12$

and,  $\frac{l_{ey}}{b} = \frac{1.3 \times 1000}{400} = 3.25 < 12$



So, it is a short column

Minimum eccentricity  $e_{min} = \frac{\text{unsupported length}}{500} + \frac{\text{lateral dimension}}{30}$

bending about x-x axis  $e_{min} = \frac{2000}{500} + \frac{600}{30} = 24 \text{ mm.} < 0.05 \times 600 = 30 \text{ mm.}$

bending about y-y axis  $e_{min} = \frac{2000}{500} + \frac{400}{30} = 17.33 \text{ mm.} < 0.05 \times 400 = 20 \text{ mm.}$

∴  $e_{min} < 0.05 \times \text{lateral dimension}$  in both direction. Therefore, strength of column is given by;

$$P_u = 0.4 f_{ck} \cdot A_c + 0.67 f_y \cdot A_{sc}$$

$$\text{or, } 1800 \times 1.5 = 0.4 \times 20 \times (400 \times 600 - A_{sc}) + 0.67 \times 415 \times A_{sc}$$

$$\therefore A_{sc} = 2888.35 \text{ mm}^2$$

$$\text{min. steel} = 0.8\% = \frac{0.8}{100} \times 400 \times 600 = 1920 \text{ mm}^2$$

$2888.35 > 1920$  so, OK.

$$\text{No. of 20 mm. dia bars} = \frac{2888.35}{314} = 9.2$$

provide 10 bars of 20 mm dia

Lateral ties:-

① Diameter  $\nless (\phi_L)_{\max} = \frac{20}{4} = 5 \text{ mm.}$

$\nless 6 \text{ mm.}$

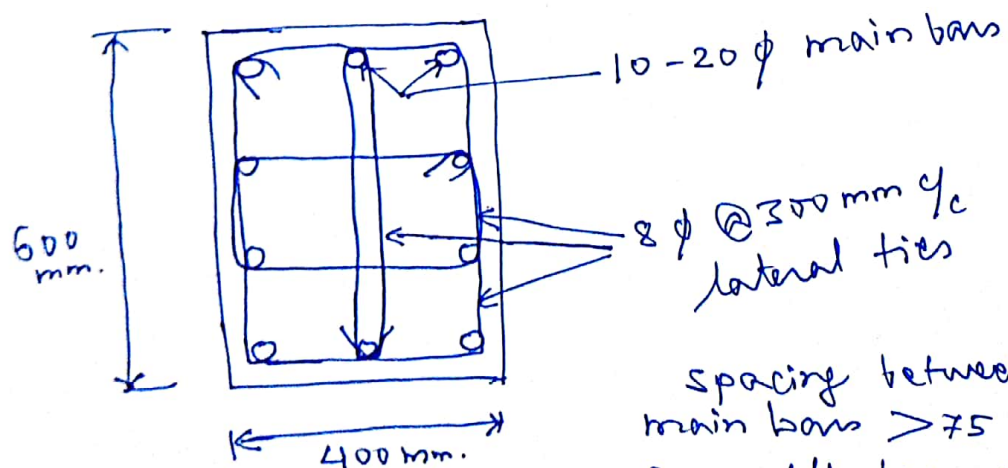
provide 8 mm.  $\phi$  ties (min. dia for Fe 415 HYSD bars = 8 mm)

② Pitch  $\nless$  least lateral dimension = 400 mm.

$\nless 16 (\phi_L)_{\min} = 16 \times 20 = 320 \text{ mm.}$

$\nless 300 \text{ mm.}$

so, provide pitch = 300 mm.



spacing between main bars  $> 75$   
so middle bars are tied in other direction also using additional ties