# Type checking $6^{\text {th }}$ sem cse 

## Type Checking

## Static Checking



- Static (Semantic) Checks
- Type checks: operator applied to incompatible operands?
- Flow of control checks: break (outside while?)
- Uniqueness checks: labels in case statements
- Name related checks: same name?


## Type Checking

- Problem: Verify that a type of a construct matches that expected by its context.
- Examples:
- mod requires integer operands (PASCAL)
-     * (dereferencing) - applied to a pointer
- a[i] - indexing applied to an array
- $f(a 1, a 2, \ldots, a n)$ - function applied to correct arguments.
- Information gathered by a type checker:
- Needed during code generation.


## Type Systems

- A collection of rules for assigning type expressions to the various parts of a program.
- Based on: Syntactic constructs, notion of a type.
" Example: If both operators of "+", "-", "*" are of type integer then so is the result.
- Type Checker: An implementation of a type system.
- Syntax Directed.
- Sound Type System: eliminates the need for checking type errors during run time.


## Type Expressions

- Implicit Assumptions:
- Each program has a type

- Types have a structure

Basic Types
Boolean
Real
Enumerations Void
Variables

Character integer
Sub-ranges
Error
Names

Type Constructors
Arrays (strings)
Records
Sets
Pointers
Functions

## Representation of Type Expressions



## Type Expressions Grammar

Type $\rightarrow \quad$ int \| float \| char \| ...
| void
| error
| name
| variable
$\}$ Basic Types
| array(size, Type)
| record( (name, Type)^)
| pointer( Type)
| tuple((Type)*)
| fcn(Type, Type) (Type $\rightarrow$ Type)
Structured
Types

## A Simple Typed Language

Program $\rightarrow$ Declaration; Statement
Declaration $\rightarrow$ Declaration; Declaration
| id: Type
Statement $\rightarrow$ Statement; Statement
| id:= Expression
| if Expression then Statement
| while Expression do Statement
Expression $\rightarrow$ literal |num | id
| Expression mod Expression
$|E[E]| E \uparrow \mid E(E)$

## Type Checking Expressions

$$
\begin{aligned}
& E \rightarrow \text { int_const } \quad\{\text { E.type }=\text { int }\} \\
& E \rightarrow \text { float_const }\{\text { E.type }=\text { float }\} \\
& E \rightarrow \text { id } \quad\{\text { E.type }=\text { sym_lookup(id.entry, type })\} \\
& E \rightarrow E_{1}+E_{2} \quad\left\{E . \text { type }=\underline{\text { if }} E_{1} \cdot \text { type } \notin\{\text { int, float }\} \mid\right. \\
& \left.E_{2} \cdot \text { type } \notin\{\text { int, float }\}\right) \\
& \text { then error } \\
& \text { else if } E_{1} \cdot \text { type }==E_{2} \cdot \text { type }==\text { int } \\
& \text { then int } \\
& \text { else float }\}
\end{aligned}
$$

## Type Checking Expressions

$$
\begin{aligned}
& E \rightarrow E_{1} \\
& {\left[E_{2}\right]} \\
& \left\{E \text {.type }=\text { if } E_{1} \text {.type }=\operatorname{array}(S, T) \wedge\right. \\
& \left.\mathrm{E}_{2} \text {.type }=\text { int then } T \text { else error }\right\} \\
& E \rightarrow{ }^{*} E_{1} \quad\left\{E \text {.type }=\text { if } E_{1} \cdot \text { type }=\operatorname{pointer}(T) \text { then } T\right. \\
& \text { else error\} } \\
& E \rightarrow \& E_{1} \\
& \left\{\text { E.type }=\operatorname{pointer}\left(E_{1} \cdot \text { type }\right)\right\} \\
& E \rightarrow E_{1}\left(E_{2}\right) \text { \{E.type }=\text { if }\left(E_{1} \text {.type }=\mathrm{fcn}(S, T) \wedge\right. \\
& \left.E_{2} \cdot \text { type }=S \text {, then } T \text { else error }\right\} \\
& E \rightarrow\left(E_{1}, E_{2}\right) \quad\left\{E \text {.type }=\operatorname{tuple}\left(E_{1} \text {.type, } E_{2} \text {.type }\right)\right\}
\end{aligned}
$$

## Type Checking Statements

$S \rightarrow i d:=E$
\{S.type := if id.type = E.type then void else error\}
\{S.type := if E.type = boolean then S1.type else error\}
$S \rightarrow$ while $E$ do $S_{1}$
\{S.type := if E.type = boolean then $\mathrm{S}_{1}$.type $\}$
\{S.type : $=$ if $S_{1}$.type $=\operatorname{void} \wedge$
$S_{2}$. type $=$ void then void else error\}

## Equivalence of Type Expressions

Problem: When in $E_{1}$.type $=E_{2} \cdot$ type?

- We need a precise definition for type equivalence
- Interaction between type equivalence and type representation
Example: $\quad$ type vector $=$ array [1..10] of real type weight $=$ array [1..10] of real var $x, y$ : vector; $z$ : weight

Name Equivalence: When they have the same name.

- $x, y$ have the same type; $z$ has a different type.

Structural Equivalence: When they have the same structure.

- $x, y, z$ have the same type.


## Structural Equivalence

- Definition: by Induction
- Same basic type
(basis)
- Same constructor applied to SE Type (induction step)
- Same DAG Representation
- In Practice: modifications are needed
- Do not include array bounds - when they are passed as parameters
- Other applied representations (More compact)
- Can be applied to: Tree/ DAG
- Does not check for cycles
- Later improve it.


## Algorithm Testing Structural Equivalence

function sequiv( $s, t$ ): boolean
\{ if ( $s \wedge t$ are of the same basic type) return true;
if $\left(s=\operatorname{array}\left(s_{1}, s_{2}\right) \wedge t=\operatorname{array}\left(\dagger_{1}, t_{2}\right)\right)$
return sequiv $\left(s_{1}, t_{1}\right) \wedge$ sequiv $\left(s_{2}, t_{2}\right)$;
if $\left(s=\operatorname{tuple}\left(s_{1}, s_{2}\right) \wedge t=\operatorname{tuple}\left(\dagger_{1}, t_{2}\right)\right)$
return sequiv $\left(s_{1}, t_{1}\right) \wedge$ sequiv $\left(s_{2}, t_{2}\right)$;
if $\left(s=f c n\left(s_{1}, s_{2}\right) \wedge t=f \operatorname{cn}\left(t_{1}, t_{2}\right)\right)$
return sequiv $\left(s_{1}, t_{1}\right) \wedge \operatorname{sequiv}\left(s_{2}, t_{2}\right)$;
if $\left(s=\operatorname{pointer}\left(s_{1}\right) \wedge t=\operatorname{pointer}\left(\dagger_{1}\right)\right)$
return sequiv $\left(s_{1}, t_{1}\right)$;

## Recursive Types

Where: Linked Lists, Trees, etc.
How: records containing pointers to similar records
Example: $\quad$ type link $=\uparrow$ cell;
cell = record info: int; next = link end

Representation:



Substituting names out (cycles)

## Recursive Types in C

- C Policy: avoid cycles in type graphs by:
- Using structural equivalence for all types
- Except for records $\rightarrow$ name equivalence
- Example:
- struct cell \{int info; struct cell * next;\}
- Name use: name cell becomes part of the type of the record.
- Use the acyclic representation
- Names declared before use - except for pointers to records.
- Cycles - potential due to pointers in records
- Testing for structural equivalence stops when a record constructor is reached $\sim$ same named record type?


## Overloading Functions \& Operators

- Overloaded Symbol: one that has different meanings depending on its context
- Example: Addition operator +
- Resolving (operator identification): overloading is resolved when a unique meaning is determined.
- Context: it is not always possible to resolve overloading by looking only the arguments of a function
- Set of possible types
- Context (inherited attribute) necessary


## Overloading Example

function "*" ( $\mathrm{i}, \mathrm{j}: \mathrm{integer)}$ return complex;
function "*" ( $x, y$ : complex) return complex;

* Has the following types:
fcn(tuple(integer, integer), integer) fcn(tuple(integer, integer), complex) fcn(tuple(complex, complex), complex)
int $\mathrm{i}, \mathrm{j}$;
$k=i^{*} j ;$

